

Brain Data

Requires “care” version 1.1.7 (November 2014) or later

This R script reproduces the analysis of brain gene expression data from V. Zuber and K. Strimmer. 2011. *High-dimensional regression and variable selection using CAR scores*. *Statist. Appl. Genet. Mol. Biol.* **10**: 34 (<http://dx.doi.org/10.2202/1544-6115.1730>)

Load “care” package and brain gene expression data set

```
library("care")
```

```
## Loading required package: corpcor
```

Load Lu et al. (2004) data set:

```
data(lu2004)
x = lu2004$x
y = lu2004$y # age
dim(x)
```

```
## [1] 30 403
```

Regularization parameters used to fit linear models:

```
reg = slm(x,y)$regularization
```

```
## Determine regression coefficients for SIZE.403 model
## Estimating optimal shrinkage intensity lambda (correlation matrix): 0.1373
## Estimating optimal shrinkage intensity lambda.var (variance vector): 0.0246
```

```
lambda = reg[1,"lambda"] # correlation shrinkage
lambda.var = reg[1, "lambda.var"] # variance shrinkage
```

Compute CAR scores to rank predictors:

```
car = carscore(x, y, lambda=lambda)
ocar = order(car^2, decreasing=TRUE)
ocar[1:30]
```

```
## [1] 73 297 262 182 336 140 362 403 389 124 239 83 244 123 148 160 212
## [18] 238 361 339 36 167 369 59 44 57 268 250 216 24
```

Fit linear models with increasing number of predictors:

```
numpred = c(seq(5, 45, by=10), seq(53, 403, by=25))
numpred
```

```
## [1] 5 15 25 35 45 53 78 103 128 153 178 203 228 253 278 303 328
## [18] 353 378 403
```

```
car.predlist = make.predlist(ocar, numpred, name="CAR")
car.models = slm(x, y, car.predlist, lambda=lambda, lambda.var=lambda.var)
```

```
## Determine regression coefficients for CAR.5 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.15 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.25 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.35 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.45 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.53 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.78 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.103 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.128 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.153 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.178 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
```

```

##
## Determine regression coefficients for CAR.203 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.228 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.253 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.278 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.303 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.328 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.353 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.378 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for CAR.403 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246

```

For comparison, use marginal correlations to rank predictors:

```

marg = carscore(x, y, lambda=lambda, diagonal=TRUE) # shrinking not actually required
omarg = order(marg^2, decreasing=TRUE)
marg.predlist = make.predlist(omarg, numpred, name="MARG")
marg.models = slm(x, y, marg.predlist, lambda=lambda, lambda.var=lambda.var)

```

```

## Determine regression coefficients for MARG.5 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for MARG.15 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for MARG.25 model

```



```

##
## Determine regression coefficients for MARG.328 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for MARG.353 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for MARG.378 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246
##
## Determine regression coefficients for MARG.403 model
## Specified shrinkage intensity lambda (correlation matrix): 0.1373
## Specified shrinkage intensity lambda.var (variance vector): 0.0246

```

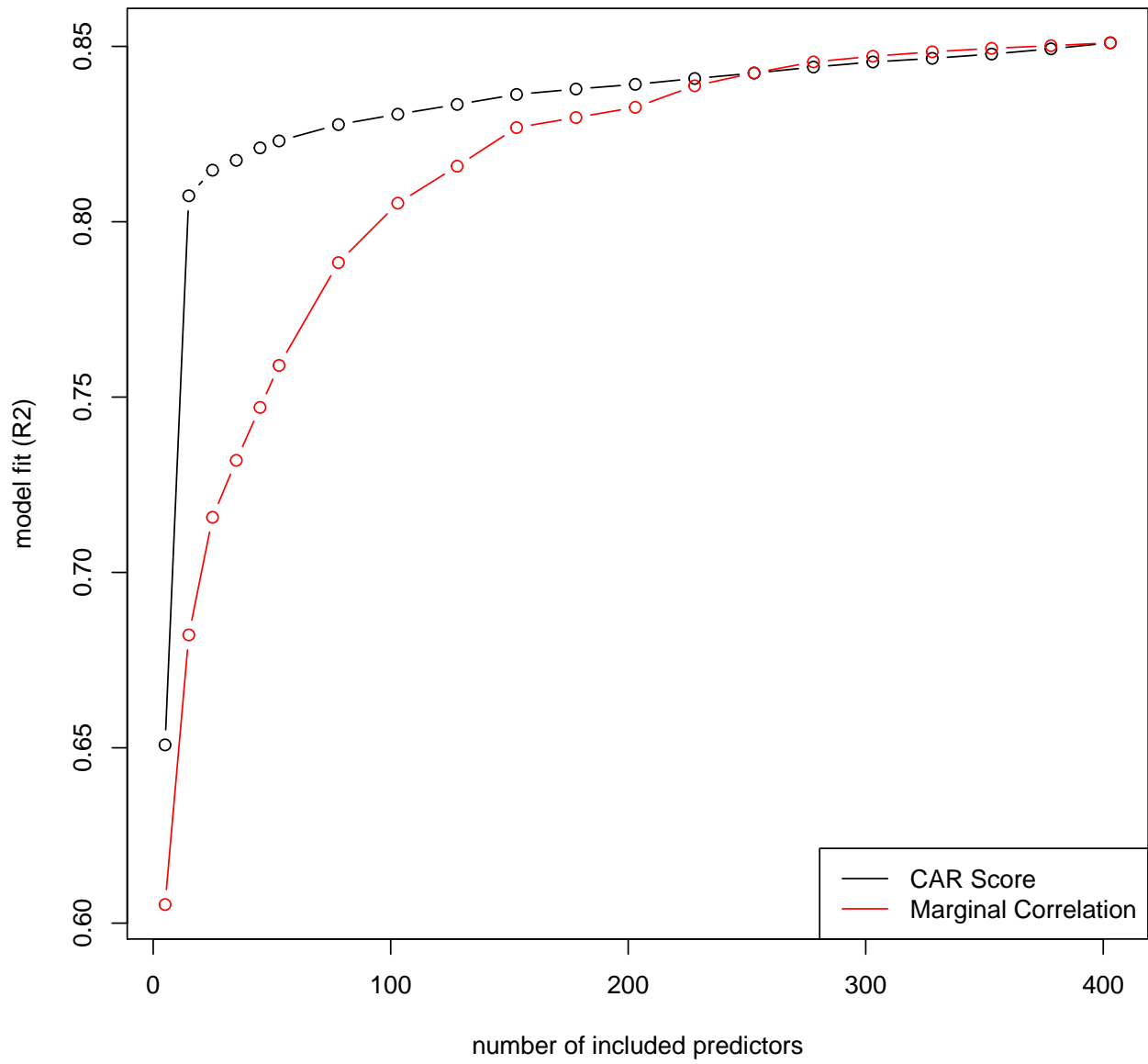
Plot model fitted R^2 for all models comparing marginal correlation with CAR scores:

```

ylim = range( c(marg.models$R2, car.models$R2) )
plot(car.models$numpred, car.models$R2, type="b", ylim=ylim,
      xlab="number of included predictors",
      ylab="model fit (R2)",
      main="CAR and Marginal Correlation Models for Brain Data")
points(marg.models$numpred, marg.models$R2, col=2, type="b")
legend("bottomright", c("CAR Score", "Marginal Correlation"), col=c(1,2), lty=c(1,1) )

```

CAR and Marginal Correlation Models for Brain Data



Estimate prediction error by crossvalidation

```
library("crossval")
```

Standardize data following Zuber and Strimmer (2011):

```
xs = scale(x)
ys = scale(y)

K=5 # number of folds
B=100 # number of repetitions
```

Rank by CAR scores, fit and predict using a specified number of predictors:

```
predfun = function(Xtrain, Ytrain, Xtest, Ytest, numVars)
{
  # rank the variables according to squared CAR scores
  car = carscore(Xtrain, Ytrain, verbose=FALSE)
  ocar = order(car^2, decreasing=TRUE)
  selVars = ocar[1:numVars]

  # fit and predict
  slm.fit = slm(Xtrain, Ytrain, predlist=list(selVars), verbose=FALSE)
  Ynew = predict(slm.fit, Xtest, verbose=FALSE)

  # compute squared error risk
  mse = mean( (Ynew - Ytest)^2)

  return(mse)
}
```

Compute results from Table 9 in Zuber and Strimmer (2011):

```
set.seed(12345)
cvp = crossval(predfun, xs, ys, K=K, B=B, numVars = 36, verbose=FALSE)
c(cvp$stat, cvp$stat.se) # 0.3441 0.0074
```

```
## [1] 0.344131632 0.007449175
```

```
set.seed(12345)
cvp = crossval(predfun, xs, ys, K=K, B=B, numVars = 60, verbose=FALSE)
c(cvp$stat, cvp$stat.se) # 0.3129 0.0066
```

```
## [1] 0.312875469 0.006584369
```

```
set.seed(12345)
cvp = crossval(predfun, xs, ys, K=K, B=B, numVars = 85, verbose=FALSE)
c(cvp$stat, cvp$stat.se) # 0.2978 0.0062
```

```
## [1] 0.297823963 0.006178467
```

This produces Figure 3 in Zuber and Strimmer (2011)

```
numpred = c(seq(10, 200, 10), 403) # number of predictors
set.seed(12345)
cvsim = lapply(numpred,
  function(i)
  {
    cat("Number of predictors:", i, "\n")
    cvp = crossval(predfun, xs, ys, K=K, B=B, numVars = i, verbose=FALSE)
    return( cvp$stat.cv )
  }
)
```

```
## Number of predictors: 10
## Number of predictors: 20
## Number of predictors: 30
## Number of predictors: 40
## Number of predictors: 50
## Number of predictors: 60
## Number of predictors: 70
## Number of predictors: 80
## Number of predictors: 90
## Number of predictors: 100
## Number of predictors: 110
## Number of predictors: 120
## Number of predictors: 130
## Number of predictors: 140
## Number of predictors: 150
## Number of predictors: 160
## Number of predictors: 170
## Number of predictors: 180
## Number of predictors: 190
## Number of predictors: 200
## Number of predictors: 403
```

```
boxplot(cvsim, names=numpred,
  col=c(rep("grey", 4), rep("white", 16), "grey"),
  main="CAR Models for the Gene Expression Data", xlab="number of included predictors",
  ylab="estimated CV prediction error")
```


CAR Models for the Gene Expression Data

